

Example 1. The area around Mount St. Helens averages about 17 earthquakes per month.

$$\begin{aligned} \text{a) } P(X=15) &= \text{poissonpdf}(17, 15) \\ &= 0.091 \end{aligned}$$

$$\begin{aligned} \text{b) } P(X \leq 10) &= \text{poissoncdf}(17, 10) \\ &= 0.049 \end{aligned}$$

$$\begin{aligned} \text{c) } P(X \geq 20) &= 1 - \text{poissoncdf}(17, 19) \\ &= 0.264 \end{aligned}$$

d) Getting exactly 80 earthquakes is most likely 0, so let's rephrase it as 80 or more.

$P(X \geq 80) = 1 - \text{poissoncdf}(17, 79) = 0$, still 0%, so either that was very rare or something was changing with Mt. Saint Helens!

Example 2 The average number of horse fatalities at each of the four major horse tracks is 17.4. Santa Anita Park in Arcadia had 41 deaths last year.

$$\begin{aligned} \text{a) } P(X \leq 10) &= \text{poissoncdf}(17.4, 10) \\ &= 0.041 \end{aligned}$$

$$\begin{aligned} \text{b) } P(X=41) &= \text{poissonpdf}(17.4, 41) \\ &= 6.04 \times 10^{-7} \\ &= 0.000000604 \\ \text{or } &= 0+ \quad \text{VERY UNLIKELY!} \end{aligned}$$

$$\begin{aligned} \text{c) } P(X \geq 41) &= 1 - \text{poissoncdf}(17.4, 41) \quad \text{should be 40} \\ &\approx 0.000001 \\ &\approx 0+ \quad \text{still very close to 0\% so something} \\ &\quad \text{is very different at Santa Anita because that} \\ &\quad \text{many deaths can't occur by random} \\ &\quad \text{chance alone!} \end{aligned}$$

Example 3 A single bank teller can help approximately 20 customers an hour. The mean number of customers a particular bank sees is 47.8 per hour.

$$\begin{aligned} \text{a) } P(x < 25) &= P(x \leq 24) \\ &= \text{poissoncdf}(47.8, 24) \\ &\approx 0.00011 \end{aligned}$$

$$\begin{aligned} \text{b) } P(x = 60) &= \text{poissonpdf}(47.8, 60) \\ &\approx 0.012 \quad \text{Not very likely.} \end{aligned}$$

$$\begin{aligned} \text{c) } P(x \geq 60) &= 1 - \text{poissoncdf}(47.8, 60) \quad \text{should be 59} \\ &\approx 0.049 \quad \text{not extremely unusual} \end{aligned}$$