


3.1 Measures of Center



"AVERAGE" → MEAN

12, 10, 15, 8, 7

$$\bar{x} = \frac{\sum x}{n}$$

$$= \frac{12+10+15+8+7}{5}$$

$$= \frac{52}{5}$$

$$\bar{x} = 10.4$$

\$ 230,000
 175,000
 225,000
 250,000
 230,000
 1,450,000
 $\Sigma x = 2,560,000$

$$\bar{x} = \frac{\sum x}{n}$$

$$= \frac{2,560,000}{6}$$

$$\bar{x} \approx 426,666.67 ?!$$

Extreme outliers can affect the mean!

THE MEDIAN "middle"

7, 8, 10, 12, 15

M = 10
 $\bar{x} = 10$

7, 8, 10, 12, 15, 16

$$\frac{10+12}{2}$$

$$= 11$$

M = 11

7, 8, 10, 12, 15, 452

M = 11

HOUSE PRICES


175000, 225000, 230000, 230000, 250000, 1450000

M = 230000

MODE → "most"

MODE = 230,000

MODE = BLUE



MIDRANGE → "middle of the range" or middle value between the min & Max

12, 10, 15, 8, 7

↑ Max
↑ min


$MR = \frac{\min + \max}{2}$
 $= \frac{7 + 15}{2}$
 $= \frac{22}{2}$
 $MR = 11$

$\bar{x} = 10.2$
 $M = 10$
~~MODE = none~~

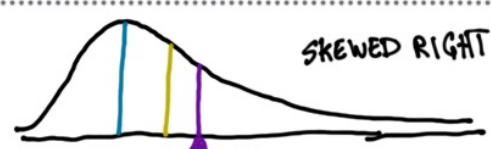
House Prices

$MR = \frac{175000 + 1950000}{2}$
 $= \$812,500$
 NOT TYPICAL!

LOCATION OF MEAN, MEDIAN, MODE, MIDRANGE



\bar{x}
M
MODE
MR



MODE
M
median
mean

SKewed RIGHT

Example 2 Instead of having the raw data above, suppose we only had the summary data:

Score	f
20 - 24	1
25 - 29	1
30 - 34	2
35 - 39	5
40 - 44	8
45 - 49	6
50 - 54	2

Class mark	f
22	1
27	1
32	2
37	5
42	8
47	6
52	2

13th value

$MR = \frac{22 + 52}{2}$
 $= 37$

Find the mean, median, and mode using the summary data and compare the values to example 1.

Mean

$$\bar{x} = \frac{\sum cm \cdot f}{n}$$

$$= \frac{22 \cdot 1 + 27 \cdot 1 + 32 \cdot 2 + 37 \cdot 5 + 42 \cdot 8 + 47 \cdot 6 + 52 \cdot 2}{25}$$

$$= \frac{1020}{25}$$

$\bar{x} = 40.8$

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$M = 42$

mode = 42

MR = 37