

## Math 146 8.3 - Testing A Claim About A Mean

### NOTATION

$\bar{x}$  = sample mean

$\mu_0$  = population mean (used in  $H_0$ )

$s$  = sample standard deviation

$\sigma$  = population standard deviation

$n$  = sample size

### t-Test for a Population Mean: $\sigma$ is NOT Known

#### REQUIREMENTS

1. The sample is a Simple Random Sample
2. The population is normally distributed **OR**  $n > 30$  (the  $t$ -test is *robust* against a departure from normality, meaning the test works reasonably well if the departure from normal isn't too extreme.)

The test statistic is given by

$$t = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$$

When calculating critical values  $t^*$  and  $P$ -values using the  $t$ -distribution, remember the degrees of freedom is  $df = n - 1$ .

**EXAMPLE 1** Oxygen tanks for SCUBA diving are to have enough oxygen for 2.1 hours of use. A sample of 6 tanks resulted in a mean time of 1.93 hours of oxygen with a standard deviation of 0.18 hours. Is there evidence at the  $\alpha = 0.02$  level that the true mean is less than 2.1 hours? (Assume normality.)

**EXAMPLE 2** Data set 3 includes samples of 106 body temperatures with a mean of 98.2°F and a standard deviation of 0.62°F. Use  $\alpha = 0.05$  to test the claim that the mean body temperature of the population is not equal to 98.6°F.

**THE CONFIDENCE INTERVAL METHOD**

Create a confidence interval using the sample data in Example 1 to test the hypotheses above. (What level confidence interval should be used?)

**EXAMPLE 3** Chuck thinks the number of keys that most people carry is less than 5. Use the data we collected at the beginning the quarter to test that claim using  $\alpha = 0.02$ . Also, use the the confidence interval method to make the same conclusion. What confidence level is necessary?

Number of keys carried:

2 2 5 1 2 3 5 4 3 10 5 3 3 1 10 4  
3 2 7 3 3 6 2 6 2 3 12 7 3 2 3 3

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**z-Test for a Population Mean:  $\sigma$  is Known** (Not very common or realistic)

In the extremely rare case where the population standard deviation  $\sigma$  is known, we can use the normal distribution with z-statistic

$$z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$$